First principles calculations of atomic structure and physical properties of calcium apatites

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Electronic structure of calcium apatites $Ca_{10}(ZO_4)_6X_2$, where Z=P, As, V; X=OH, F, CI was investigated by quantum-mechanical modelling methods in the density functional theory (DFT) in the generalized gradient approximation (GGA) and LMTO-approximation using the ABINIT package. It was shown that $Ca_{10}(PO_4)_6Cl_2$ and $Ca_{10}(PO_4)_6F_2$ organizes in space group $P6_3/m$, but not in $P6_3$. Small deviations of the total energy per unit cell indicate that the anions F-and CI-stored relative lability position on the axes of the sixth order. Phonon density of states for all series apatite $Ca_{10}(PO_4)_6X_2$, where X = F, CI, OH, have a distinct band character with different length of the individual sub-bands. The first band contains most vibrational states and is localized in the range of wave vectors from 0 to 370 cm⁻¹, the second band – from 380 to 500 cm^{-1} , the third band is localized in $600-800 \text{ cm}^{-1}$, and the fourth – $800-1150 \text{ cm}^{-1}$. The first, second and third bands correspond to the vibrations of the PO_4 tetrahedra in the apatite, the frequencies of which are in good agreement with the experimental phonon frequencies of isolated PO_4 tetrahedron. Also, the dielectric tensor and the elastic constants of calcium apatite are calculated.