

Probing the Dirac Electrons in Condensed Matter: Graphene and Topological Insulators

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Brookhaven National Laboratory, Upton, NY, USA*

Dirac Electrons in Condensed Matter: A Photoemission View

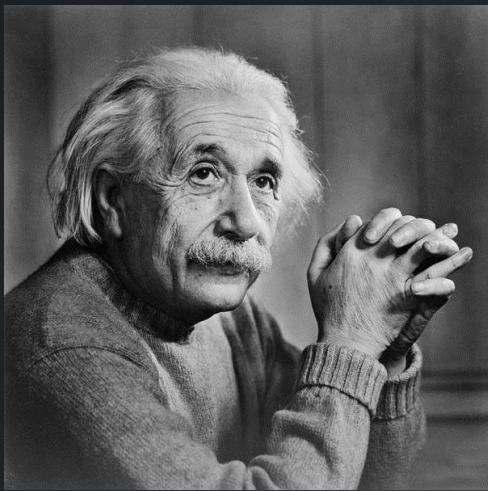
- ARPES
- Graphene
 - Nearly neutral
 - Heavily doped
 - Superconductivity
- Topological Insulators
 - Spin structure
 - Elastic scattering
 - Inelastic scattering

Angle Resolved Photoemission Spectroscopy (ARPES) - ideal probe of electronic structure

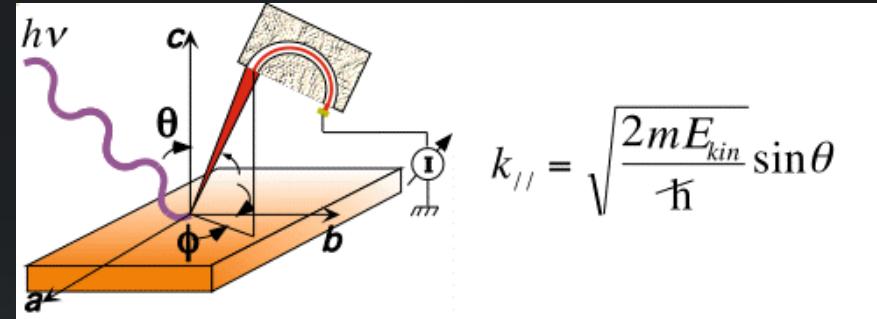
- Interesting (interacting) stuff is sometimes difficult to detect!



Hertz



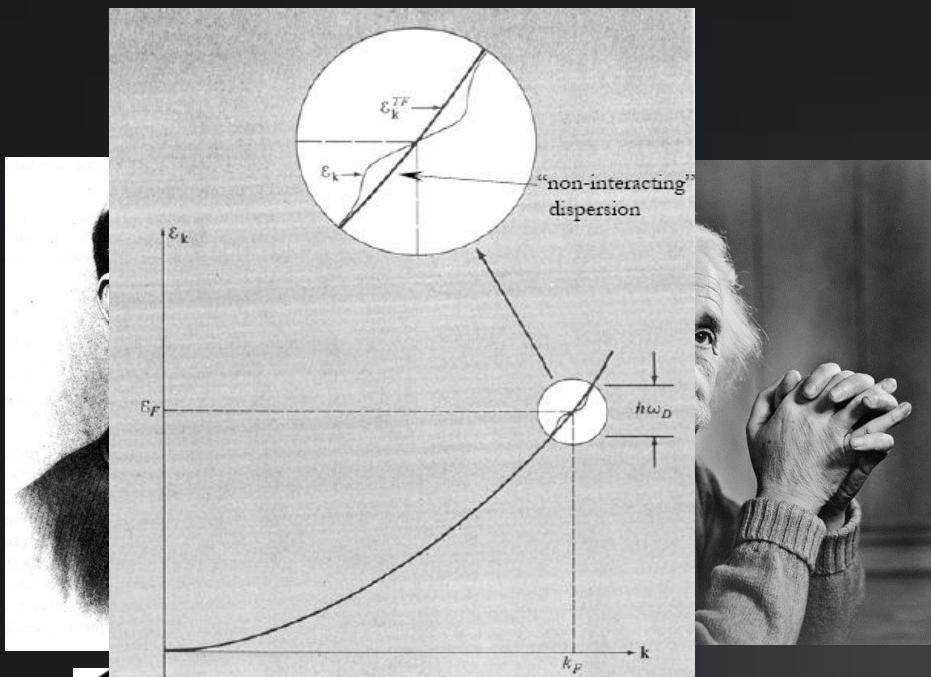
Einstein



- Band structure mapping, for a long, long time... even though it measures $\text{Im}G(k,\omega)$

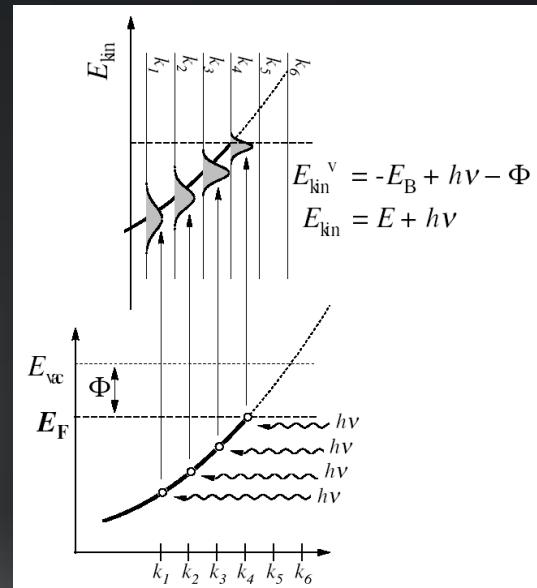
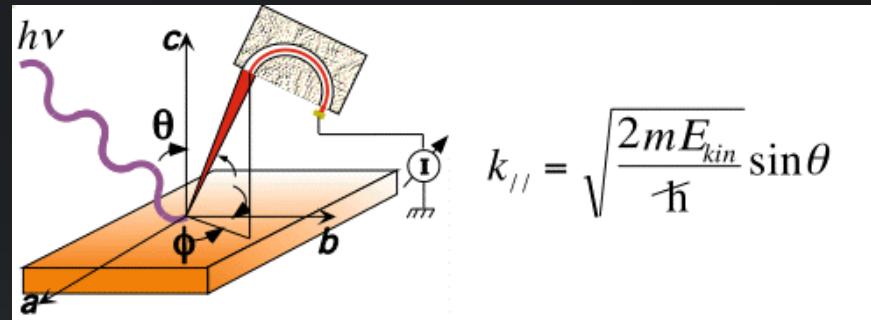
Angle Resolved Photoemission Spectroscopy (ARPES) - ideal probe of electronic structure

- Interesting (interacting) stuff is sometimes difficult to detect!



Einstein

Ashcroft/Mermin textbook "Solid State Physics"

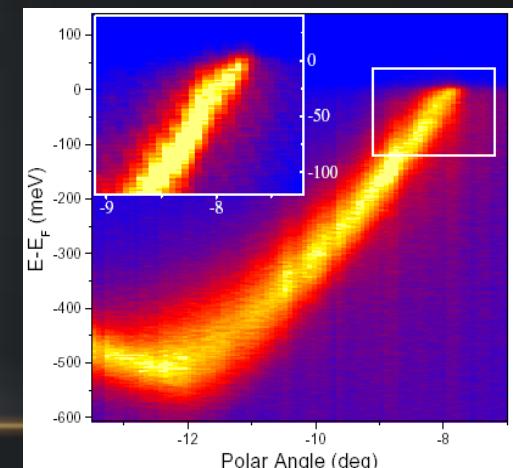
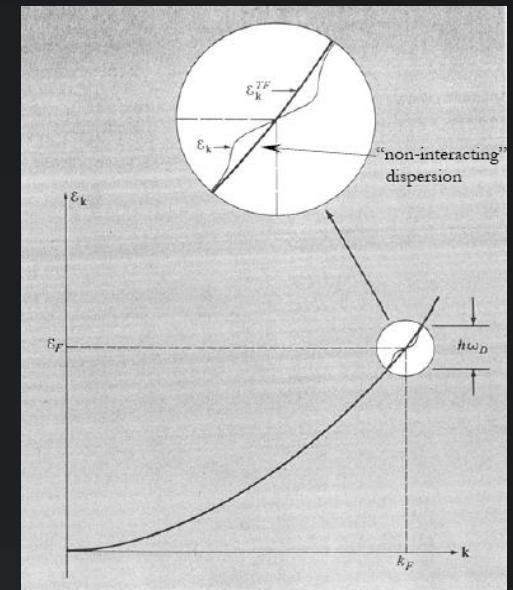
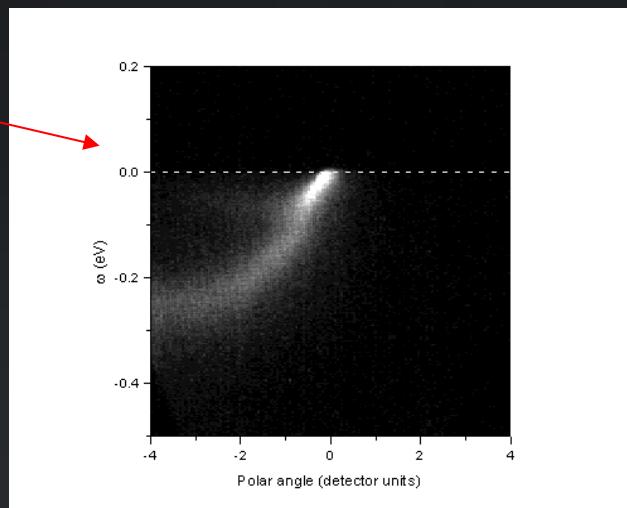
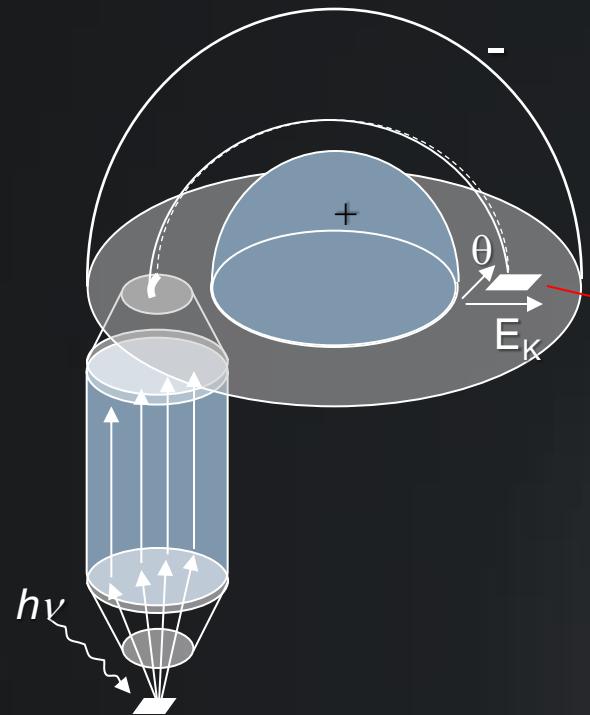


ARPES: $I(k, \omega) \propto A(k, \omega) \sim \text{Im}G(k, \omega)$

2D detection - revolution in ARPES

BNL group made a break-through in 1998:

2-Dimensional detection, high energy and angle resolution



Resolution:

- $\Delta E \sim 1-20$ meV
- $\Delta \theta \sim 0.1-0.2^\circ \rightarrow \Delta k \sim 0.005-0.01 \text{\AA}^{-1}$ at ~ 15 eV photon energy
- (< 1 meV)

T. Valla *et al*, Phys. Rev. Lett. **83**, 2085 (1999).

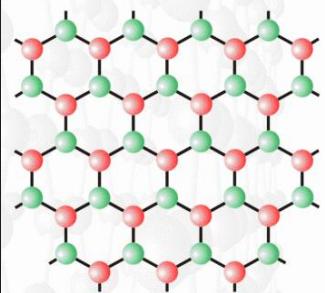
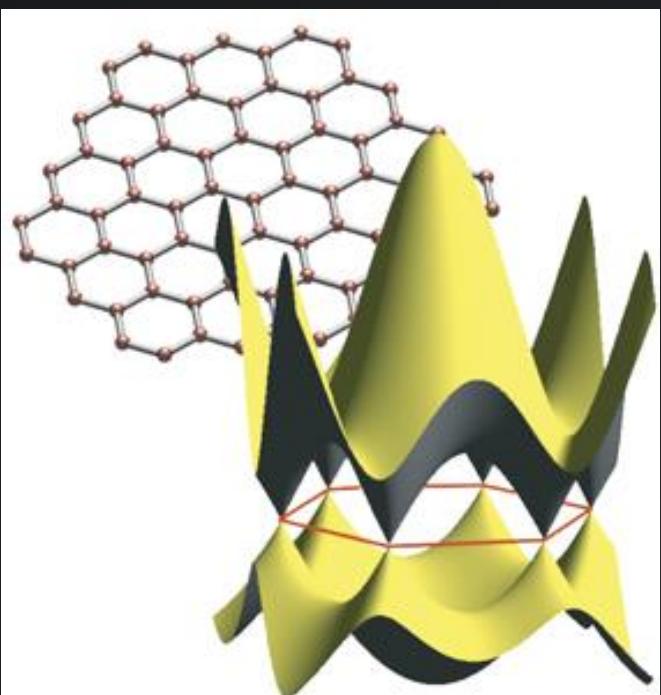
Graphene's electronic structure

1) neutral (E_D at E_F)

Massless fermions

$$E(\pm q) \approx \pm v_F |q|$$

- QHE (even at RT)
- Huge mobilities, ballistic transport on a ~micron scale
- candidate for devices, electronics, spintronics, detectors...

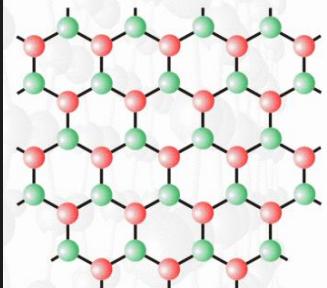
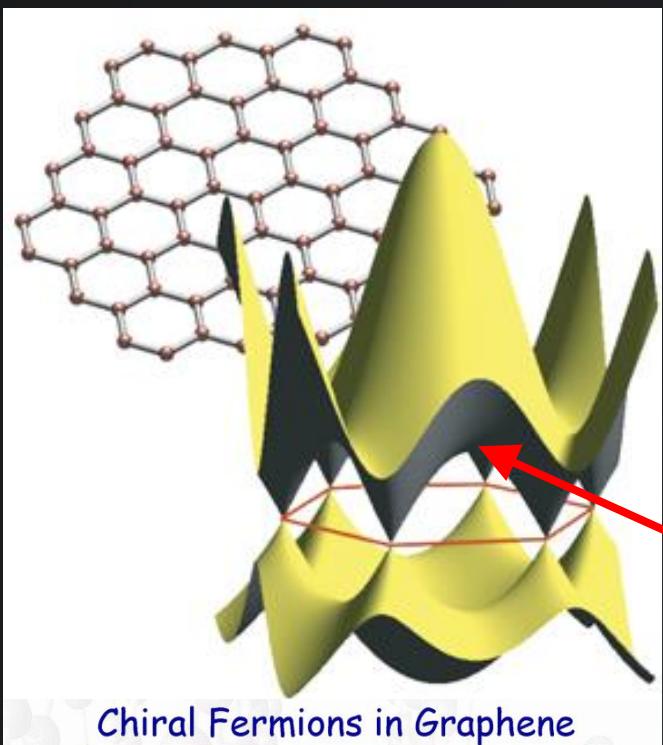


Dirac equation:

$$\hat{H} = v_F \begin{pmatrix} 0 & \hat{p}_x + i\hat{p}_y \\ \hat{p}_x - i\hat{p}_y & 0 \end{pmatrix} = v_F \vec{\sigma} \cdot \vec{p}$$



Graphene's electronic structure



Dirac equation:

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1) neutral (E_D at E_F)



Massless fermions

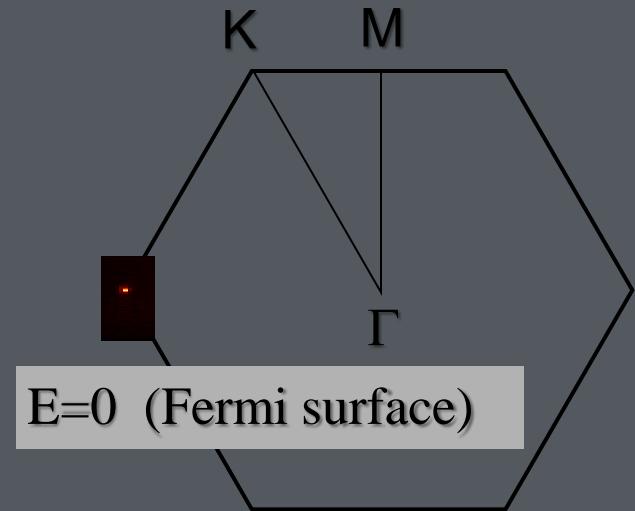
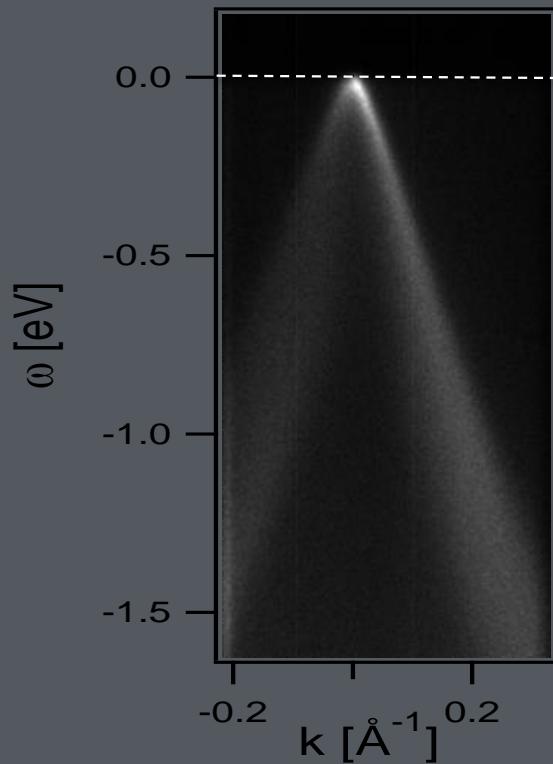
$$E(\pm q) \approx \pm v_F |q|$$

2) heavily doped (vHS at E_F)
(~1/2 e⁻ per C)

massive fermions,

large DOS, strong interactions,
superconductivity?

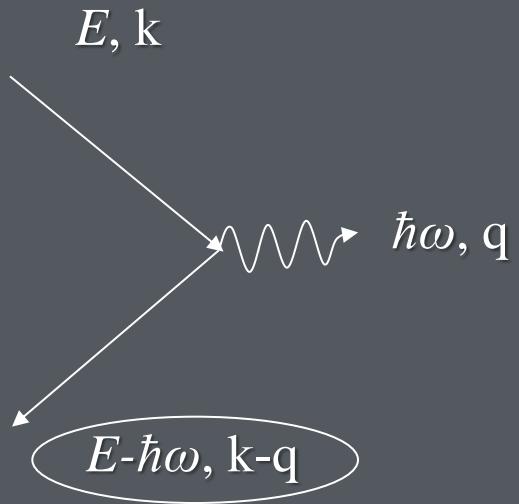
\sim Neutral regime: ARPES



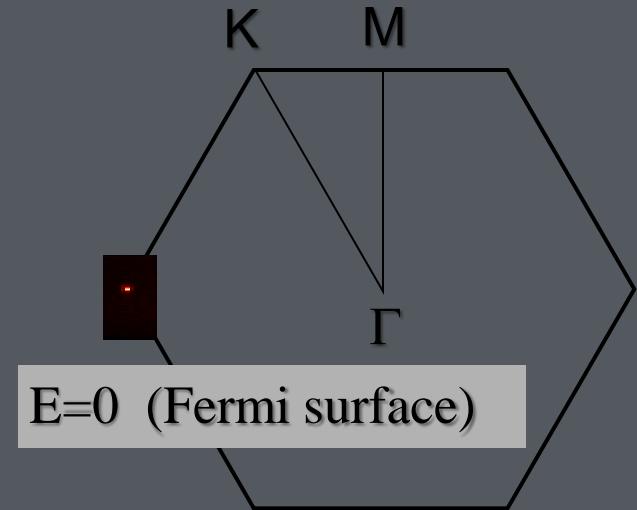
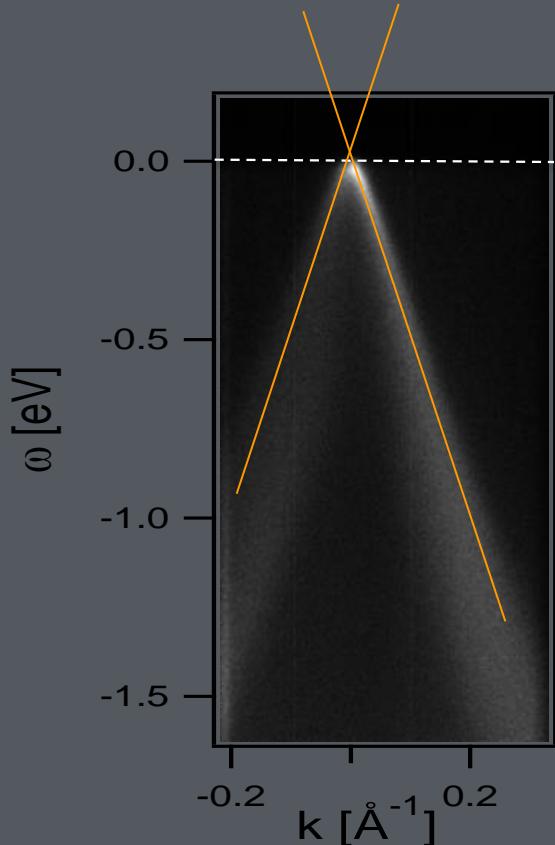
gr/SiO₂/Si

- 1) Dirac point \sim at the Fermi level
- 2) Weak electron-phonon coupling

\sim Neutral regime: ARPES



Restricted to a \sim point



- 1) Dirac point \sim at the Fermi level
- 2) Weak electron-phonon coupling

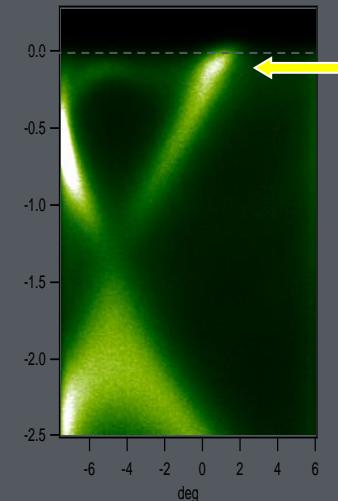
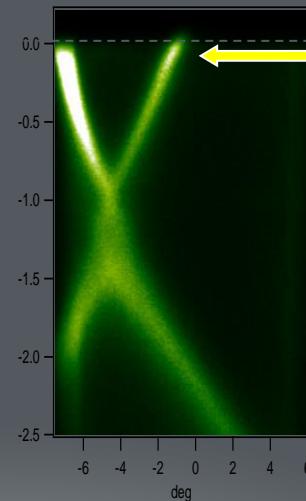
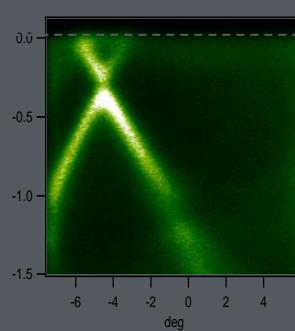
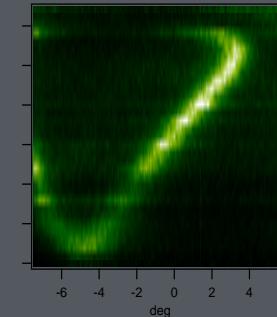
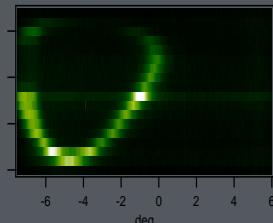
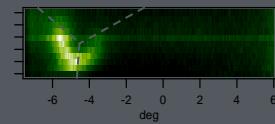
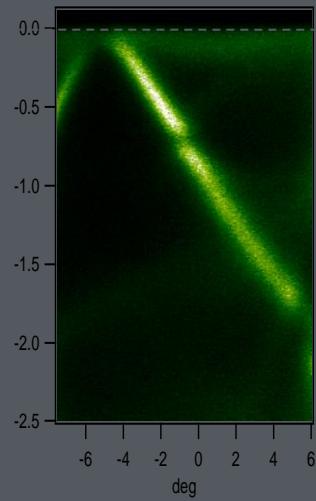
Heavy doping - graphene/Ir(111)

Graphene/Ir(111)

Li

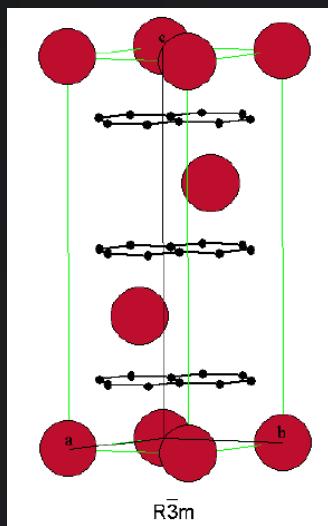
Na

more Na

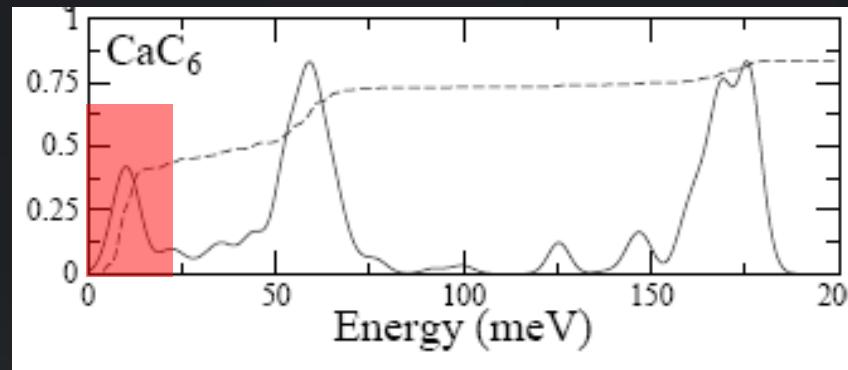


As FS grows, el-ph coupling strengthens!

Superconductivity in CaC_6 ("heavily doped graphene")



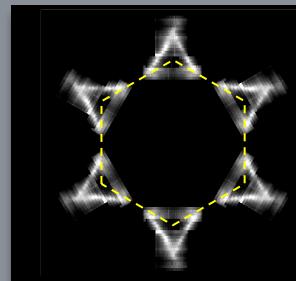
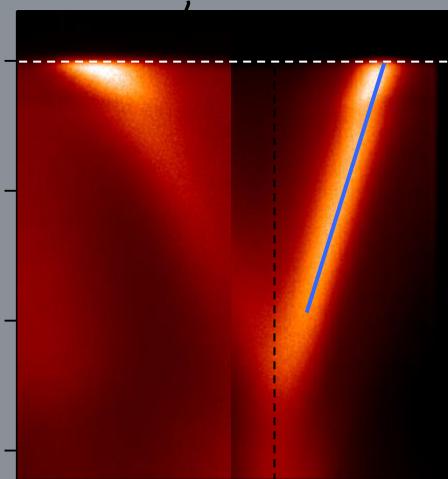
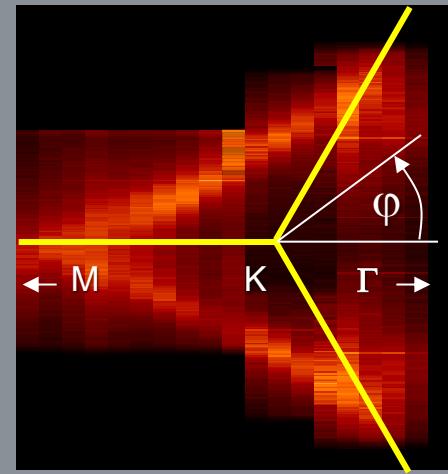
Superconducting, $T_c \sim 11.6\text{K}$!



M. Calandra and F. Mauri, Phys. Rev. Lett. 95, 237002 (2005).

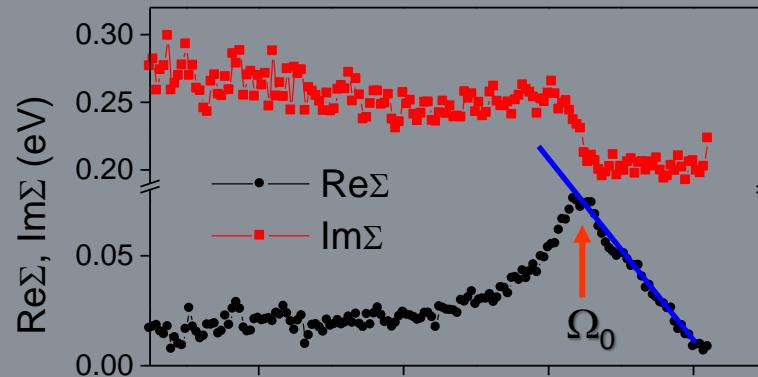
Theories: intercalate states couple to intercalate phonons
⇒ Graphene sheets unimportant!

Experiment:

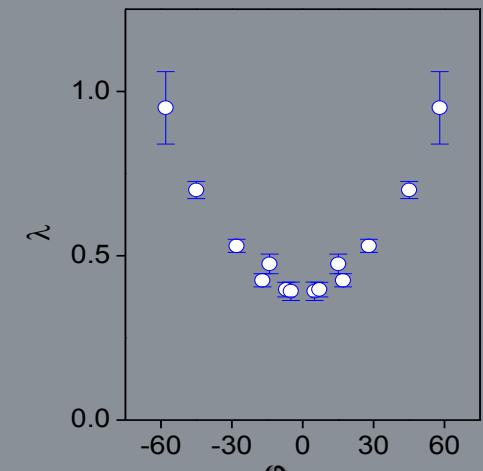
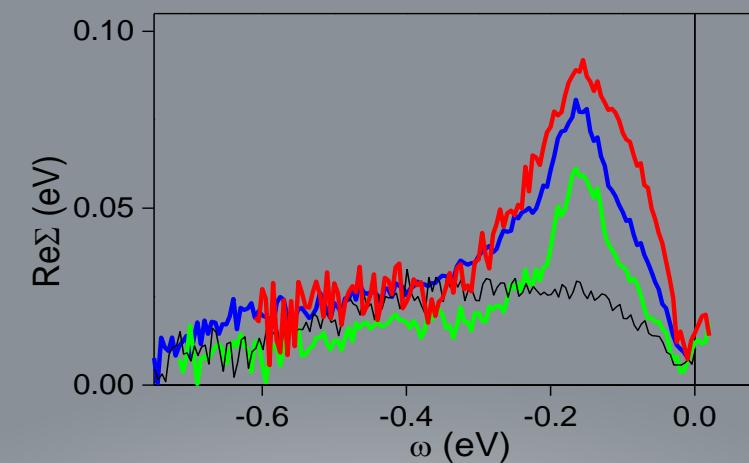


T. Valla, J. Camacho *et al*, Phys. Rev. Lett. 102, 107007 (2009)

k -resolved!



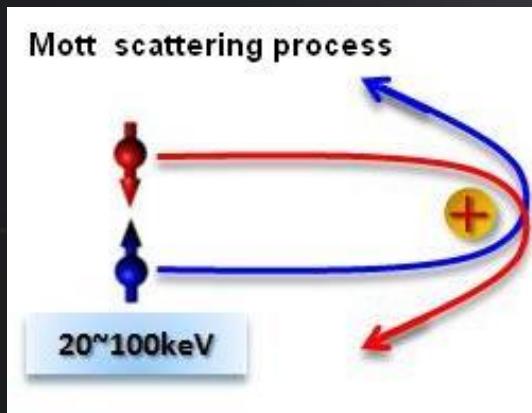
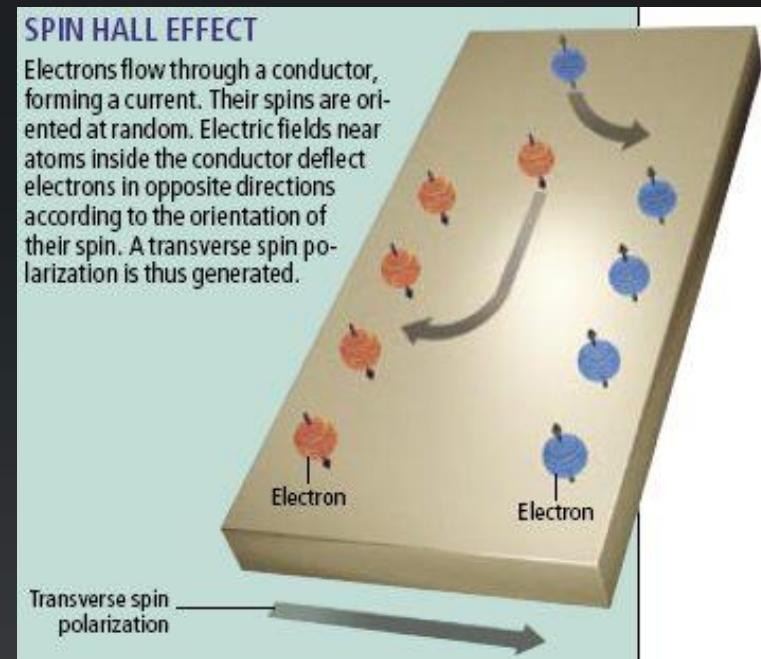
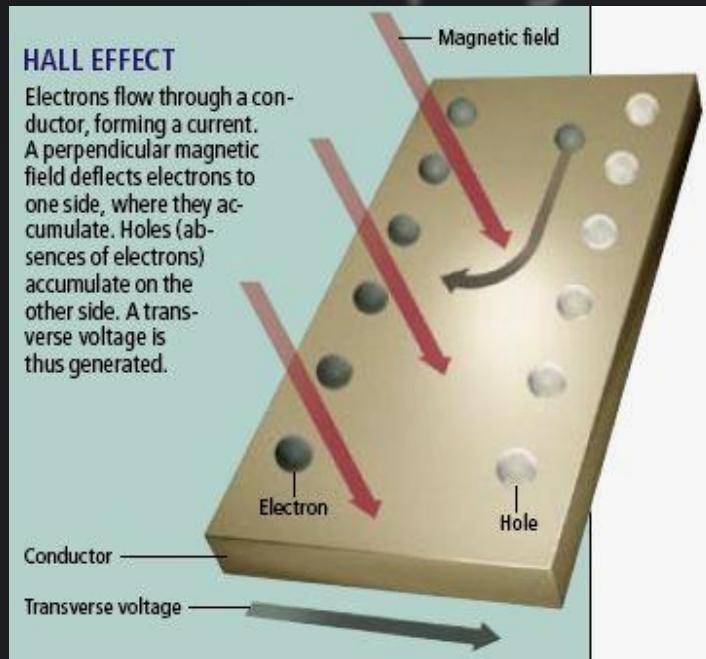
$$\lambda = -\frac{\partial \text{Re}\Sigma}{\partial \omega}$$



ARPES experiments: graphene states couple to graphene phonons
⇒ Graphene sheets responsible for SC!

Topological Insulators

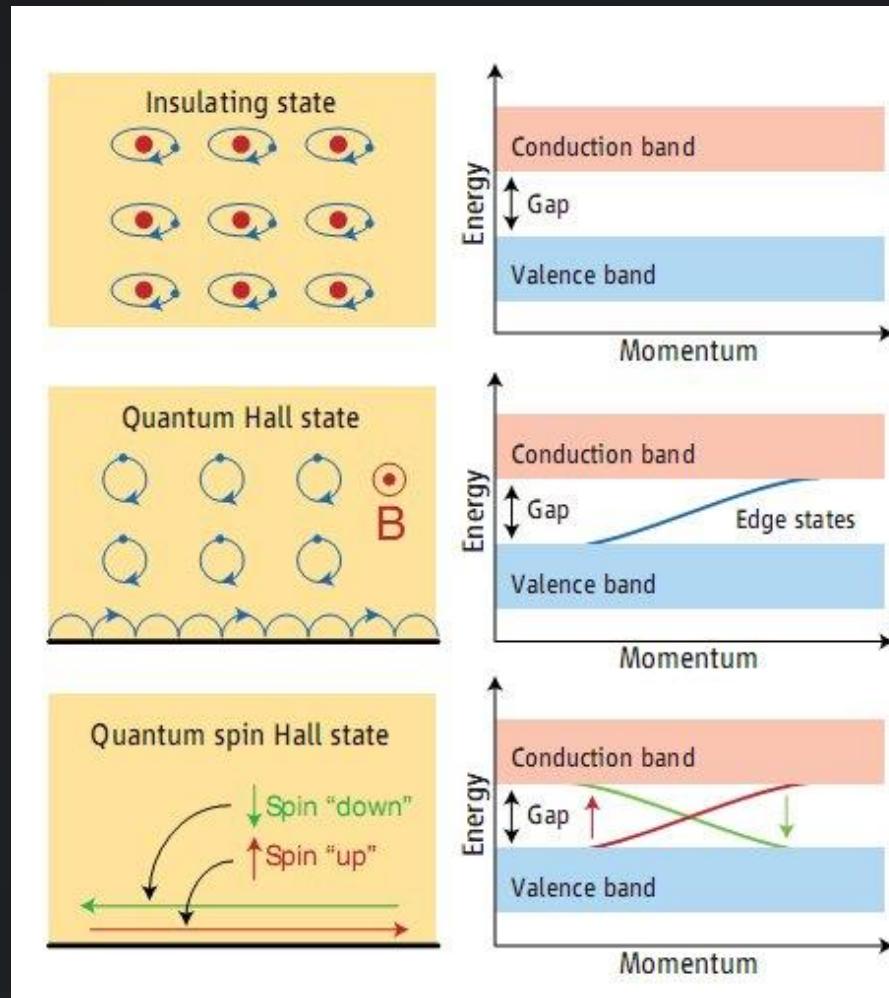
Spin-orbit coupling



SHE: spins separate without magnetic field

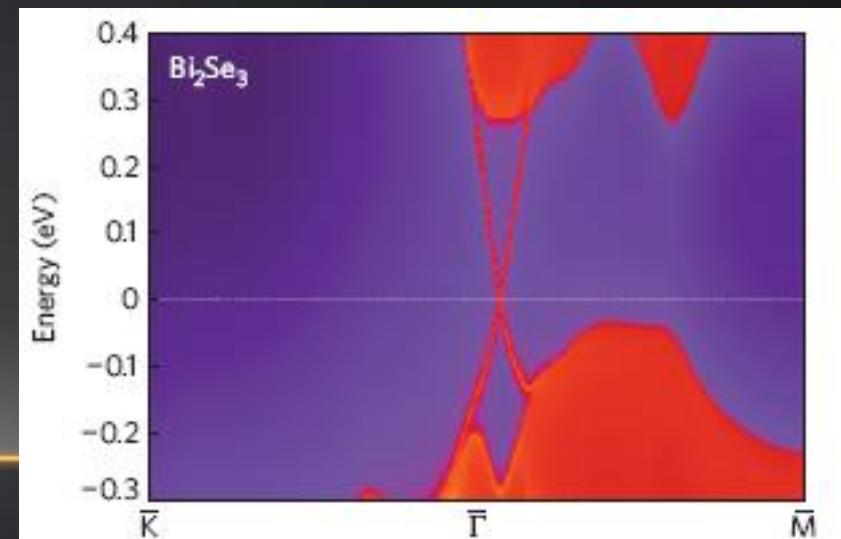
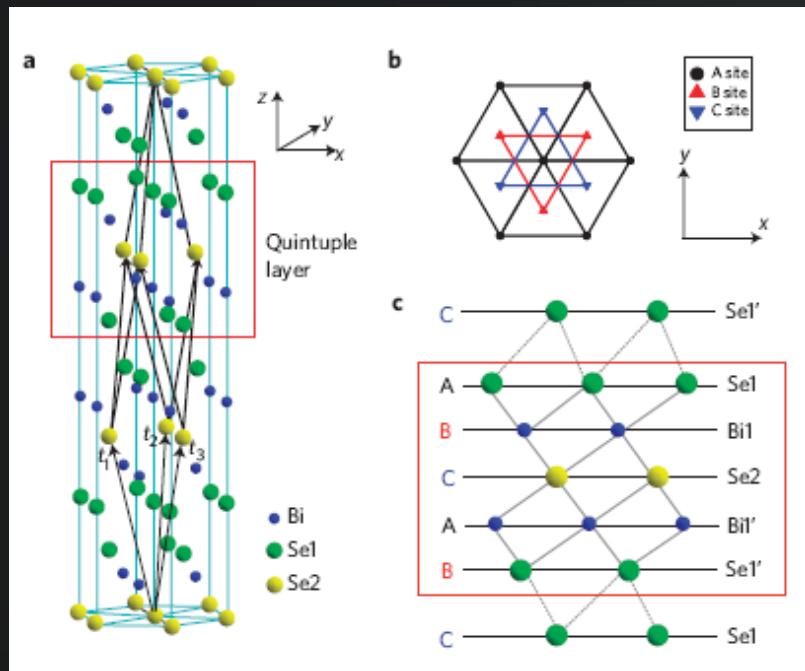
$$H_{SO} = \frac{\hbar}{4m_0^2 c^2} \mathbf{p}(\boldsymbol{\sigma} \times \nabla V(\mathbf{r}))$$

Topological Insulators:



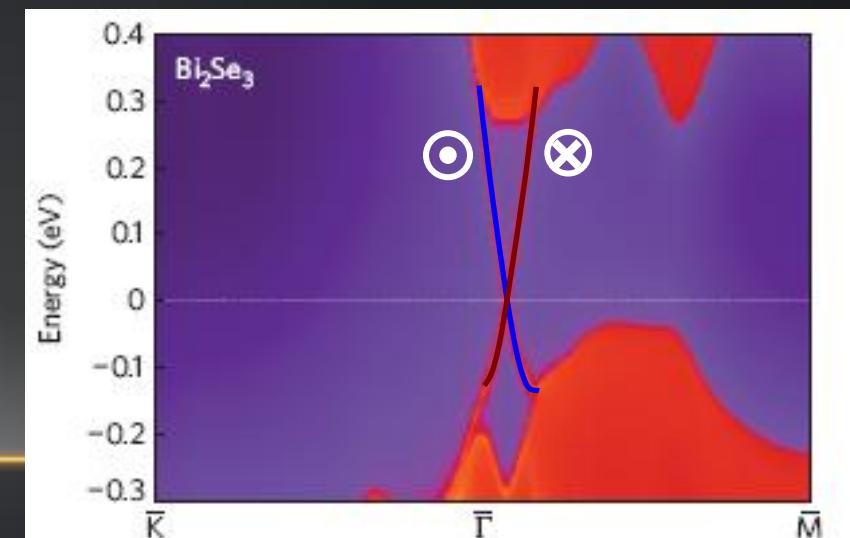
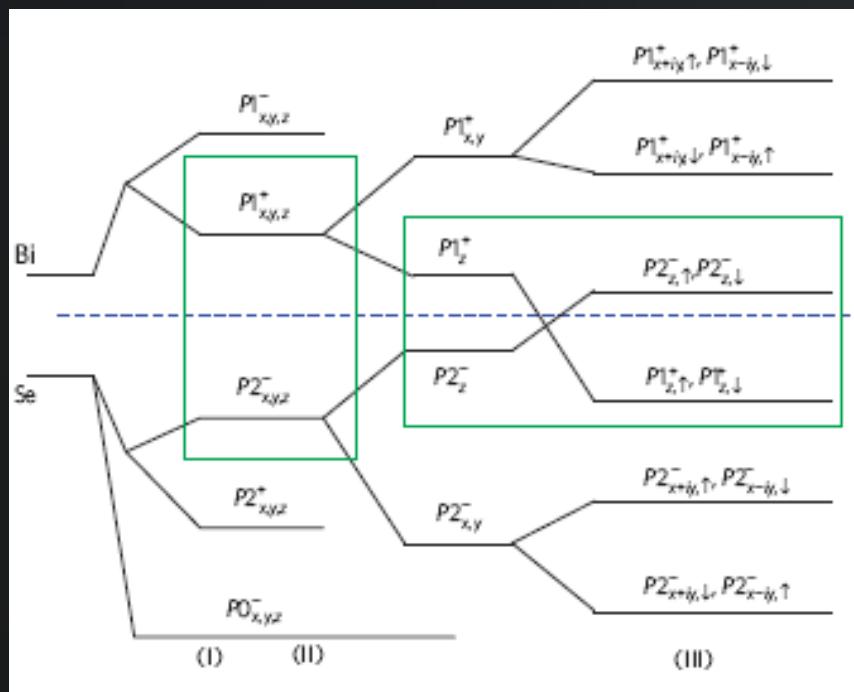
Topological Gapless States on Surfaces of Topological Insulators

- "band inversion" due to spin-orbit coupling → topological insulator
- boundary states
- spin-helical surface states on a 3D topological insulator
- topologically protected



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Topological Gapless States on Surfaces of Topological Insulators

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Theories:

➤ TI/trivial insulator:

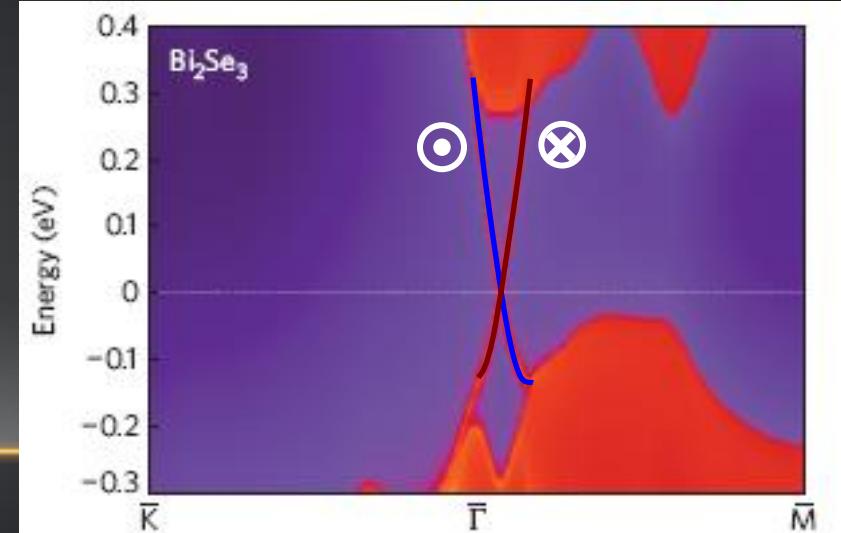
gapless, dissipationless states

➤ TI/ferromagnet:

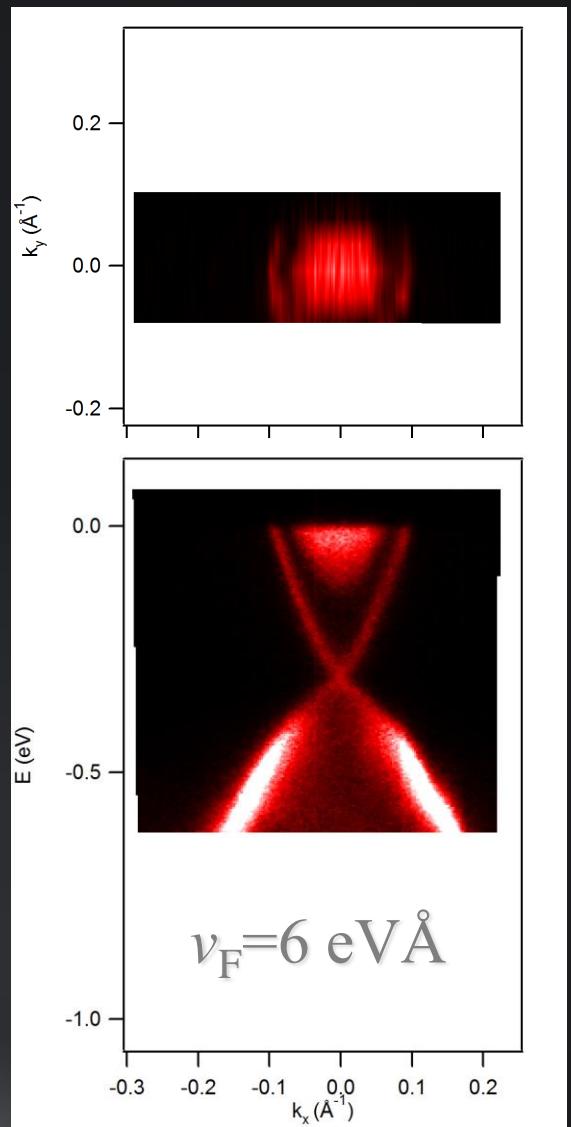
"magnetic monopoles"

➤ TI/superconductor:

Majorana fermions...



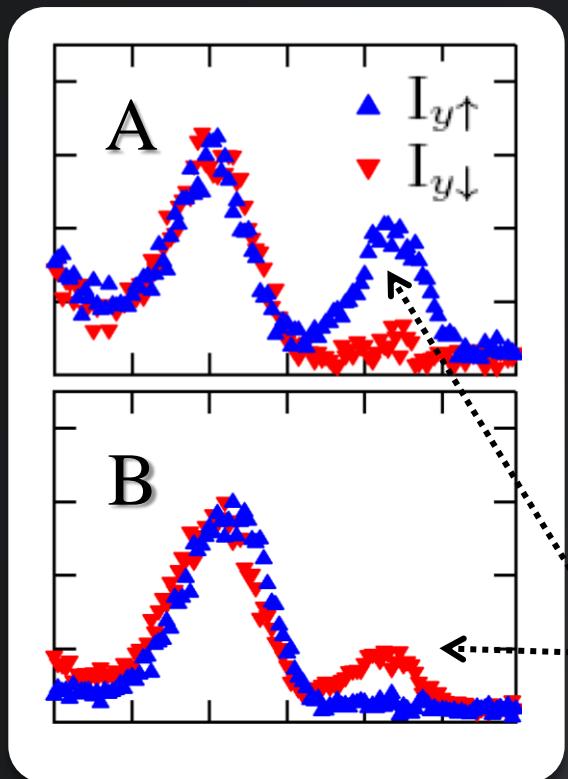
Experiments (Bi_2Se_3):



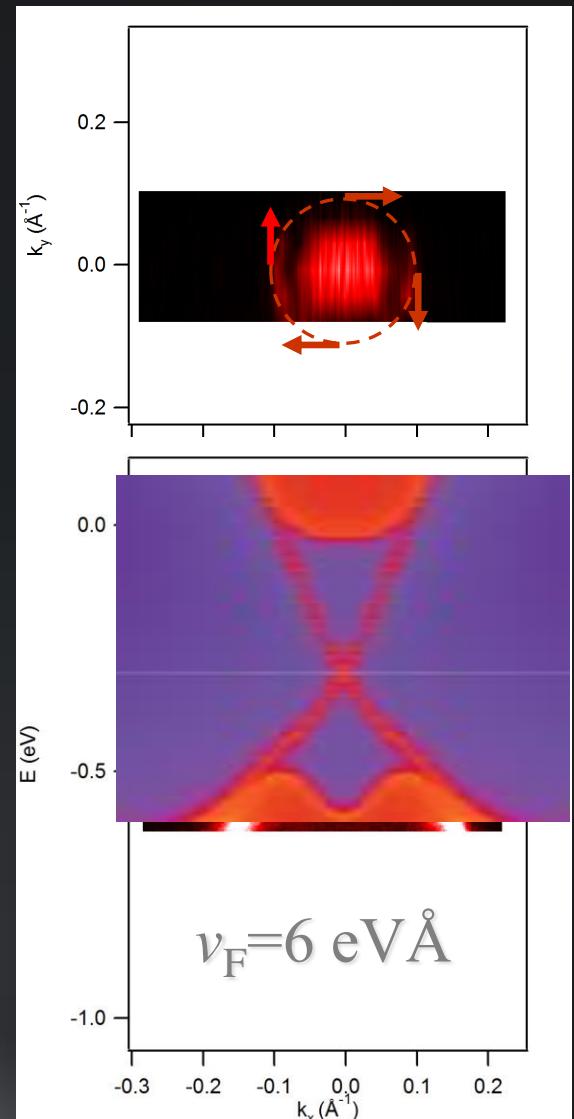
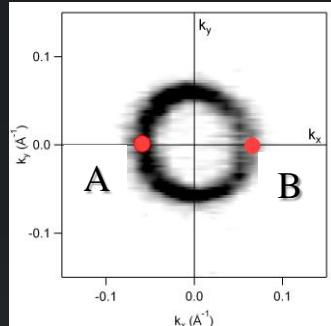
H.-J. Noh *et al*, EPL 81, 57006 (2008), (Bi_2Te_3)
D. Hsieh *et al*, NATURE 452, 970 (2008)....

Experiments (Bi_2Se_3):

Backscattering forbidden!



Z.-H. Pan *et al.*, PRL 106, 257004 (2011)



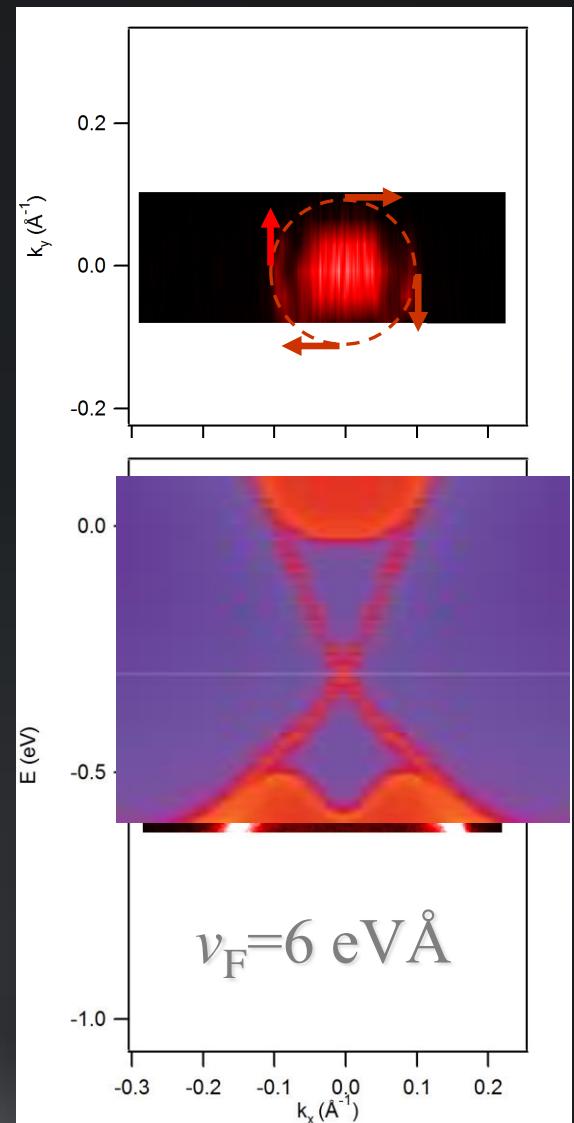
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Experiments (Bi_2Se_3):

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Interband
scattering? Inelastic
scattering?

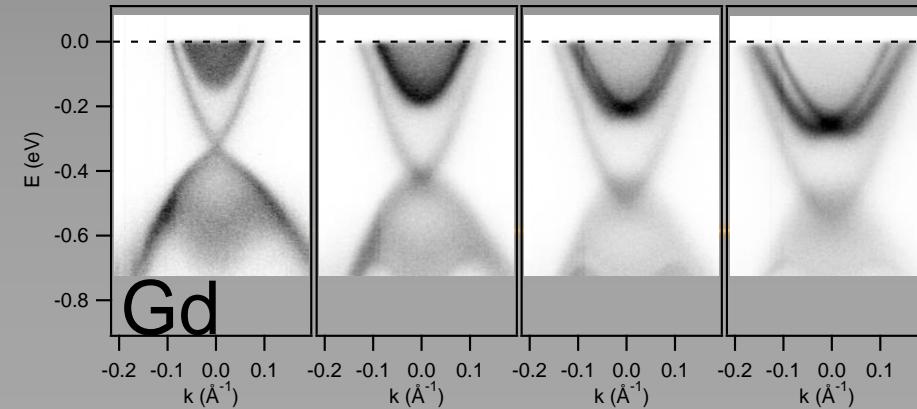
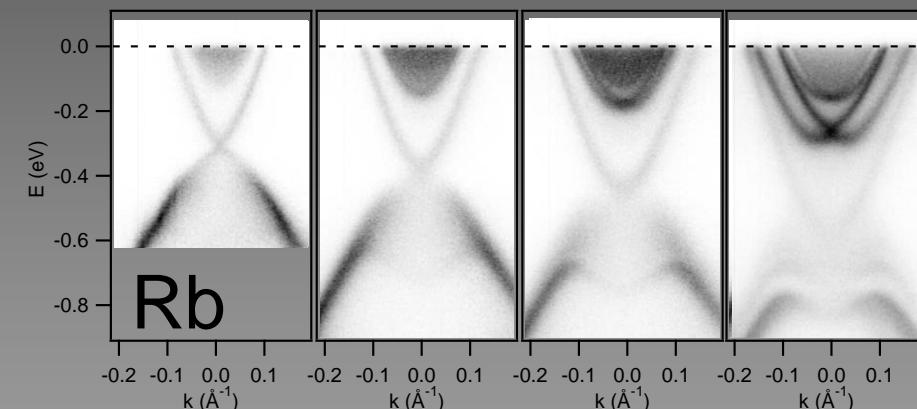
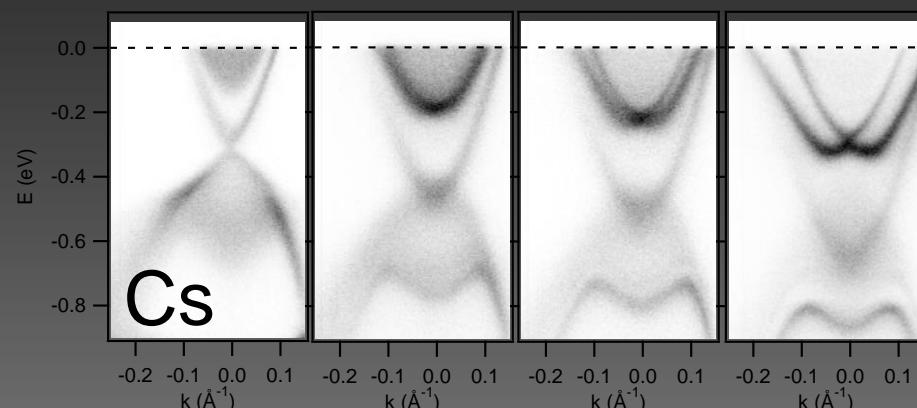


H.-J. Noh *et al*, EPL 81, 57006 (2008), (Bi_2Te_3)
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Elastic Scattering

Impurities on Bi_2Se_3 surface

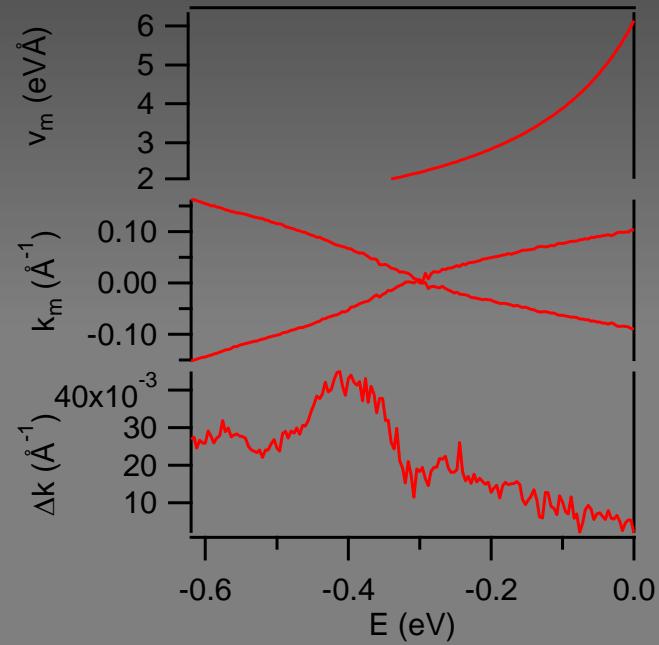
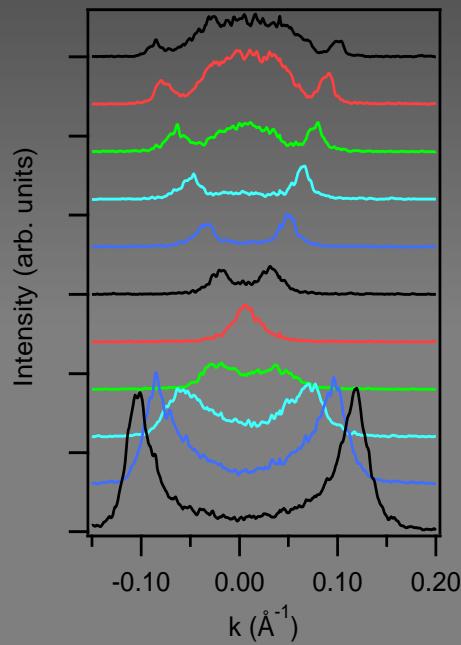
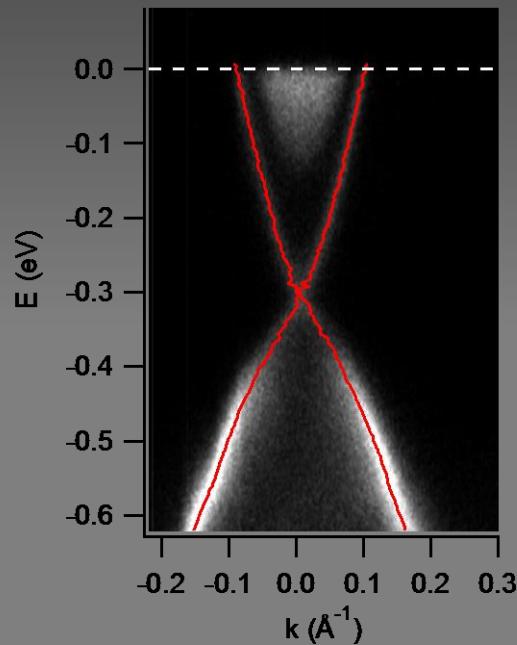
T. Valla, *et al*, PRL (2012).



Non-magnetic
impurities

Magnetic impurities!
 $(\mu \approx 8 \mu_B)$

Scattering rates from ARPES

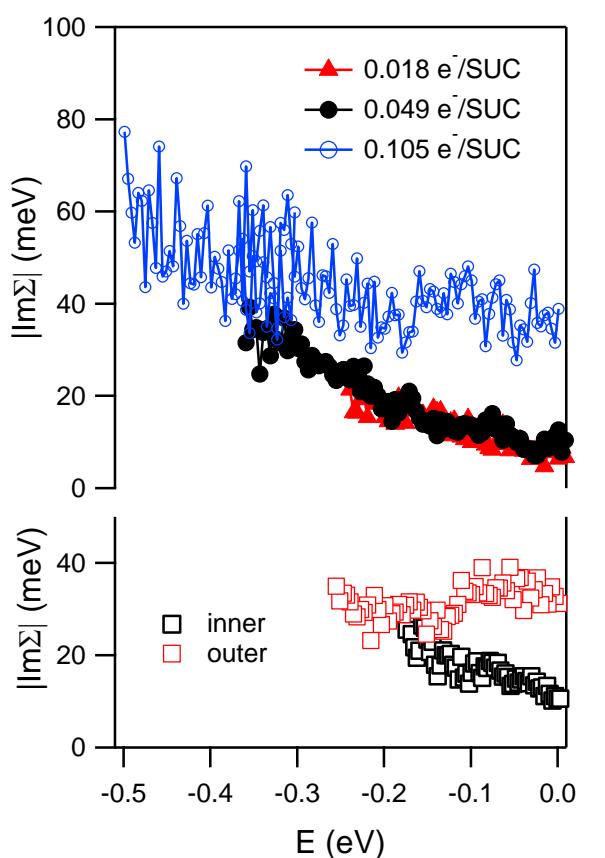


MDCs

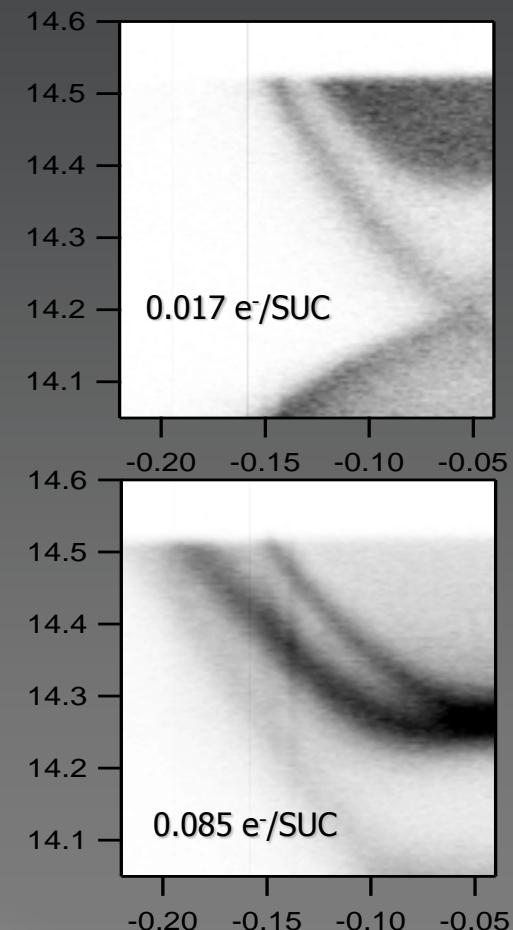
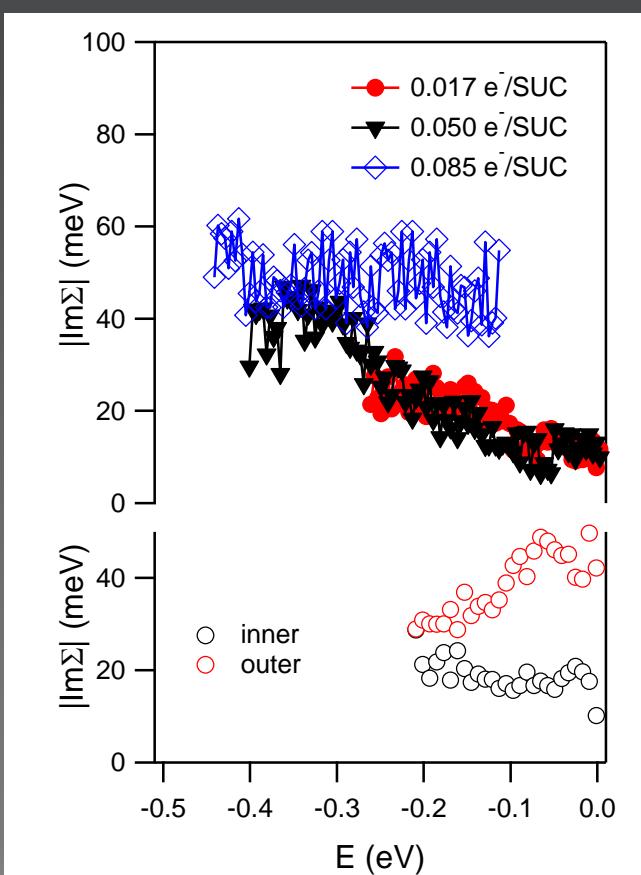
$$\Gamma = 2|\text{Im}\Sigma| = \Delta k v_m$$

Scattering rates:

Rb

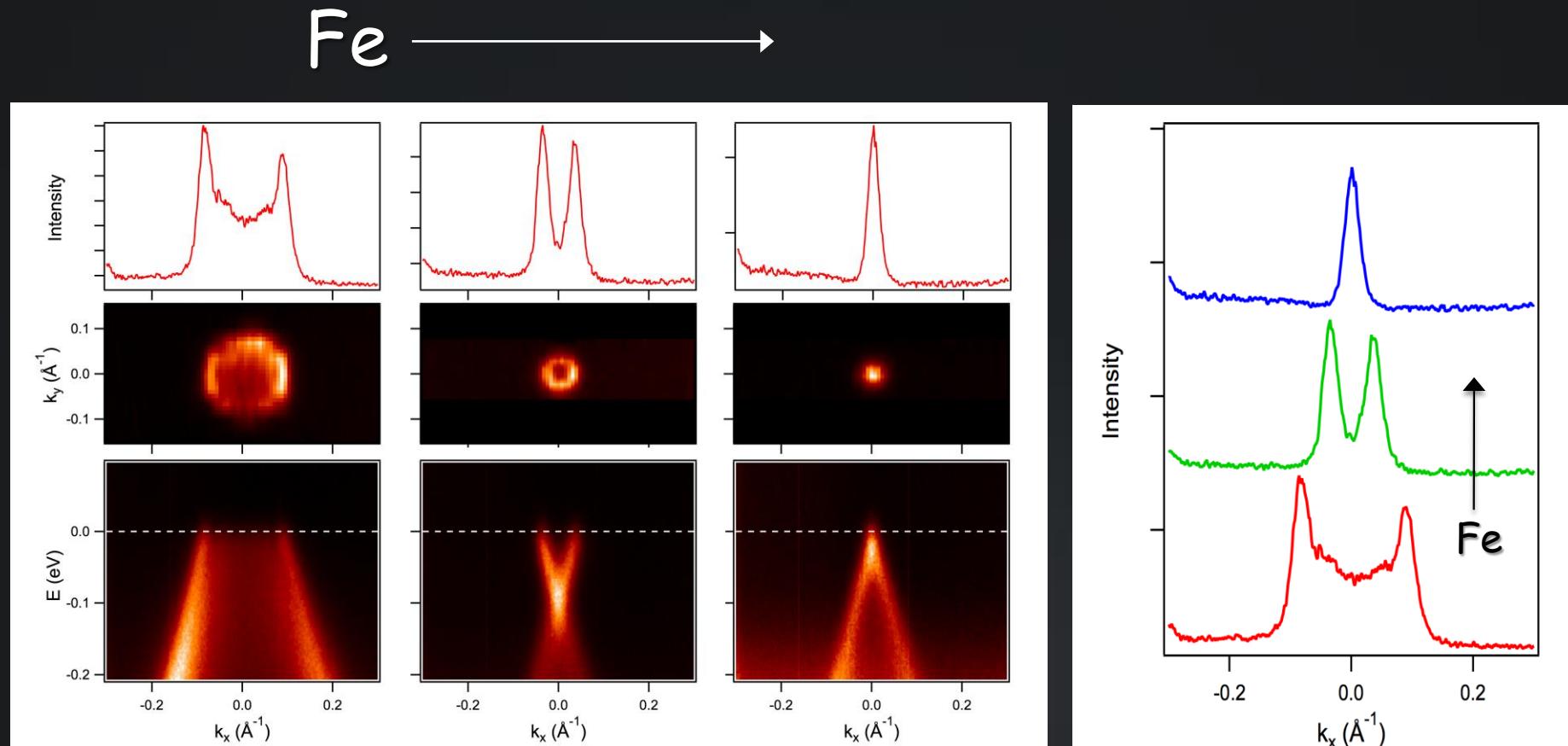


Gd



But, what about spin-flip?

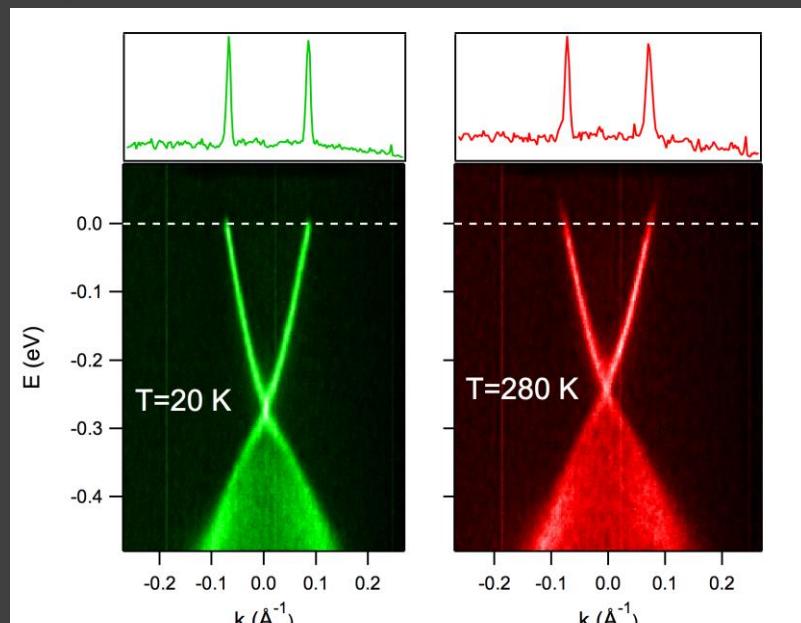
Magnetic impurities on Sb_2Te_2Se (p-type)



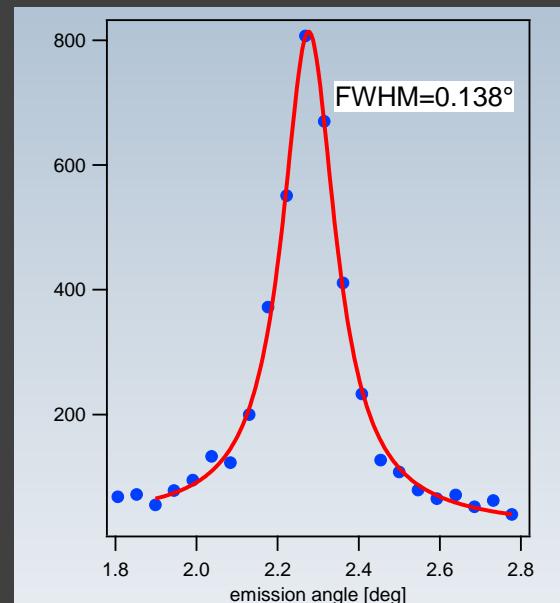
width the same - scattering the same!

Inelastic scattering

T-dependence and (a lack of) the electron-phonon coupling



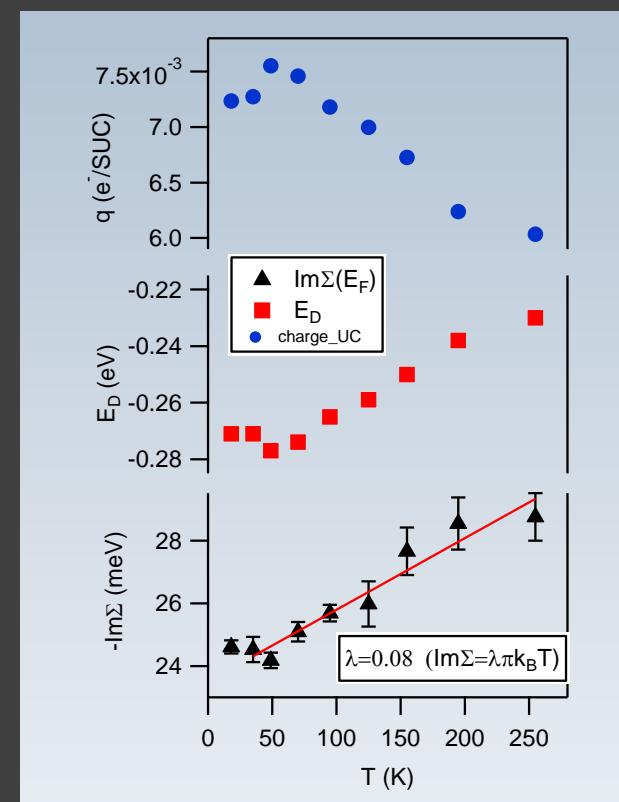
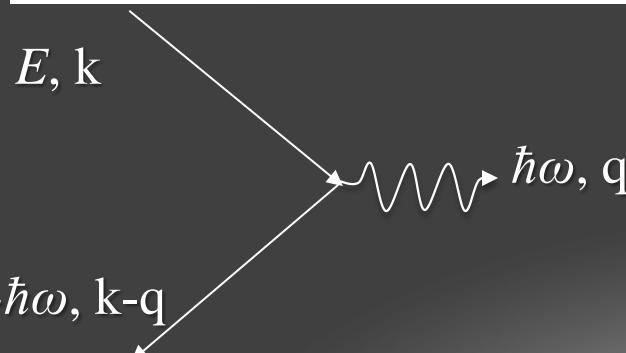
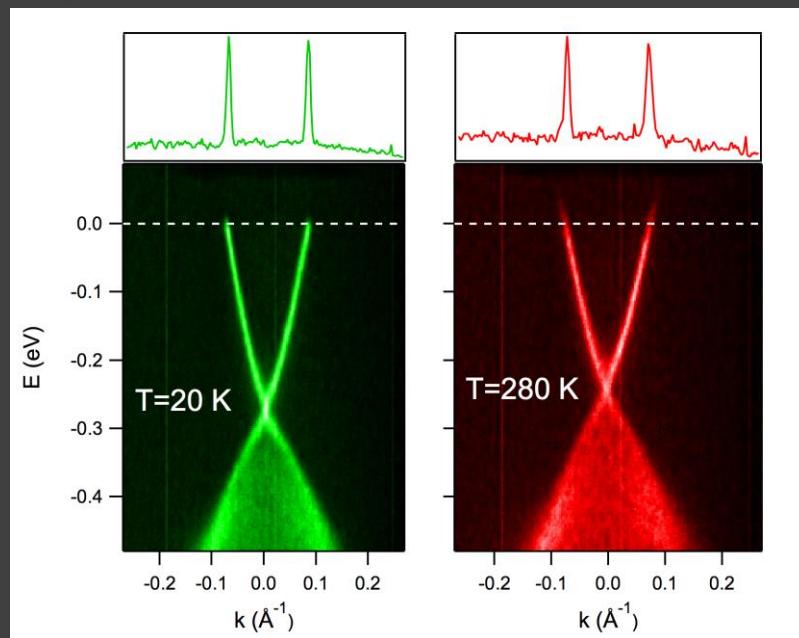
Z.-H. Pan, *et al*, Phys. Rev. Lett. **108**, 187001 (2012).



Inelastic scattering

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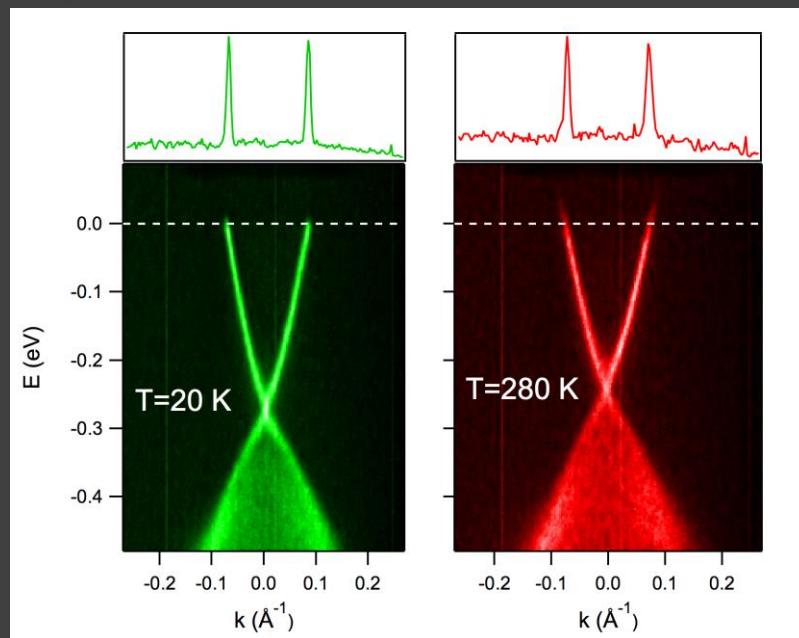
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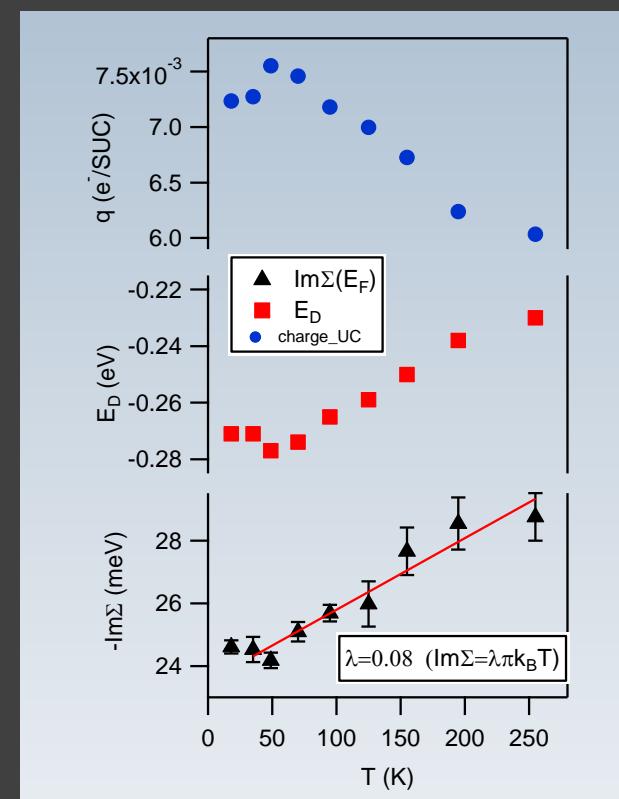
$$\text{Im}\Sigma(\omega, T) = \pi \int_0^\infty \alpha^2 F(\nu) [2n(\nu) + f(\nu + \omega) + f(\nu - \omega)] d\nu \quad \text{Im}\Sigma(0, T) \approx \pi \lambda k_B T \quad \lambda = 0.076$$

Inelastic scattering

T-dependence and (a lack of) the electron-phonon coupling



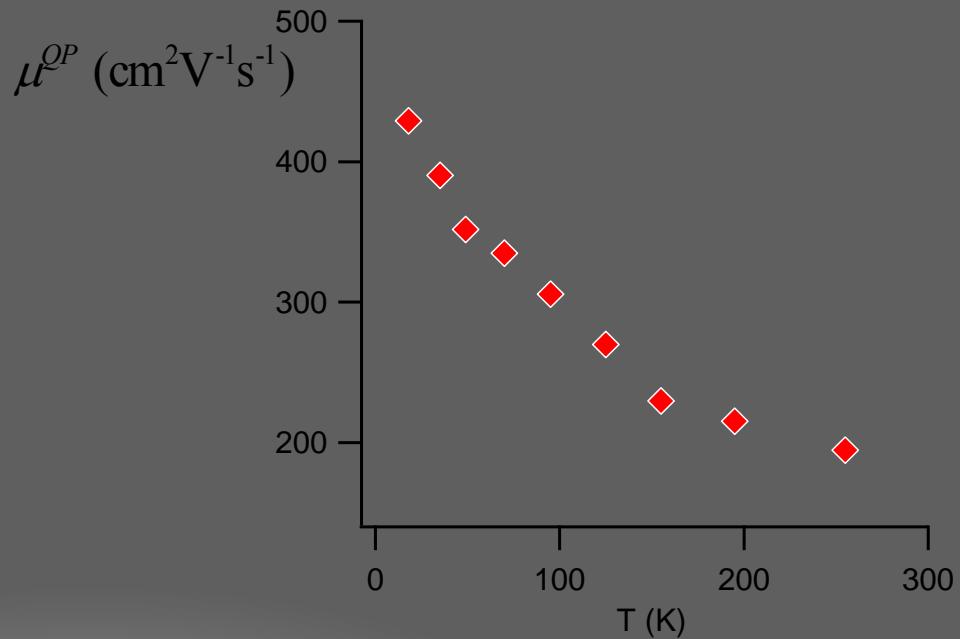
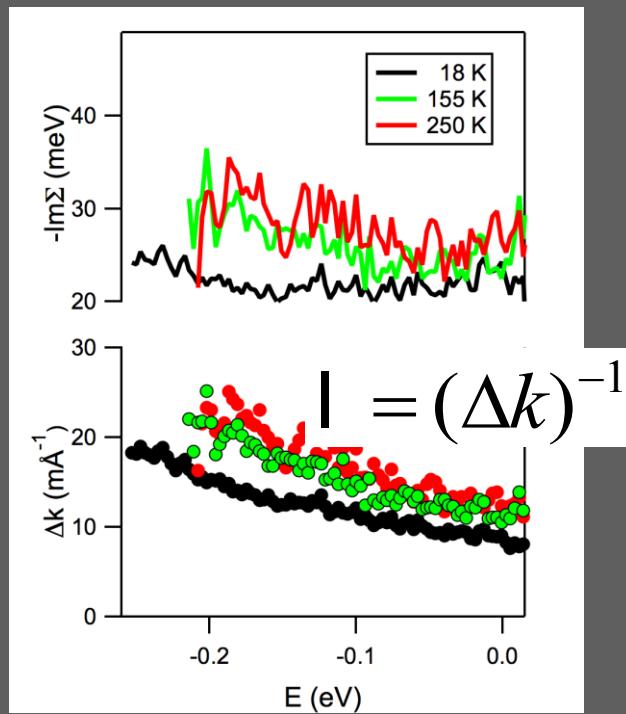
Z.-H. Pan, *et al*, Phys. Rev. Lett. **108**, 187001 (2012).



States coherent even at RT!

Relation to transport

Z.-H. Pan, *et al*, PRL, (2012).



$$\mu = \frac{e\ell_{tr}}{\hbar k_F}$$

Huge mobilities - backscattering forbidden
(but only for pristine surfaces)

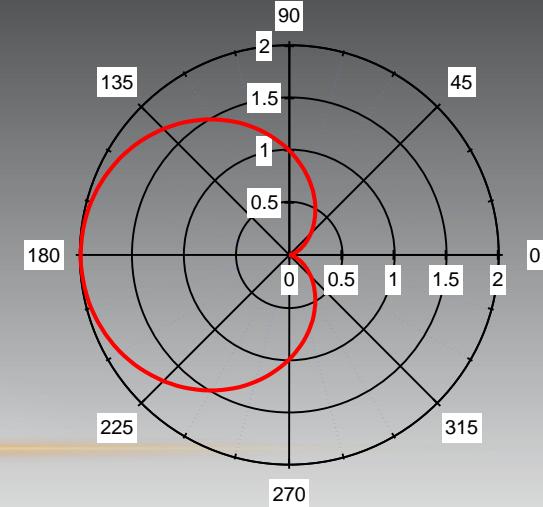
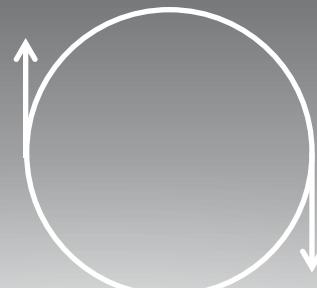
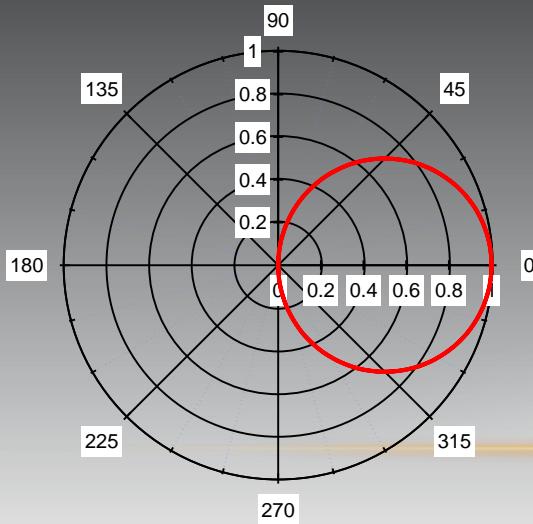
Relation to transport

$$\Gamma(k) = 1/\tau(k) = 2\pi n_i \int \frac{d^2 k'}{(2\pi)^2} \delta(\varepsilon_k - \varepsilon_{k'}) |T_{kk'}|^2$$

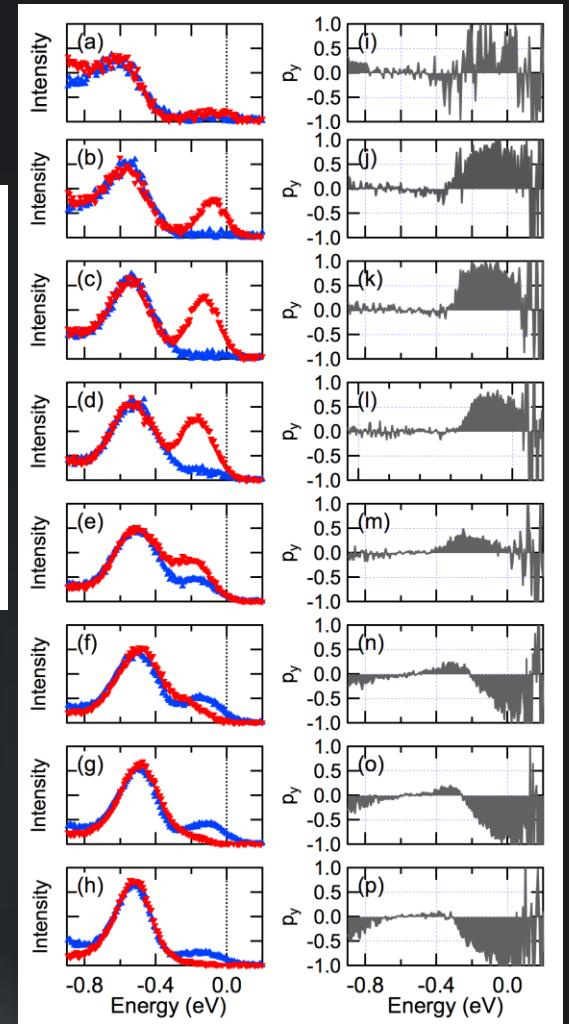
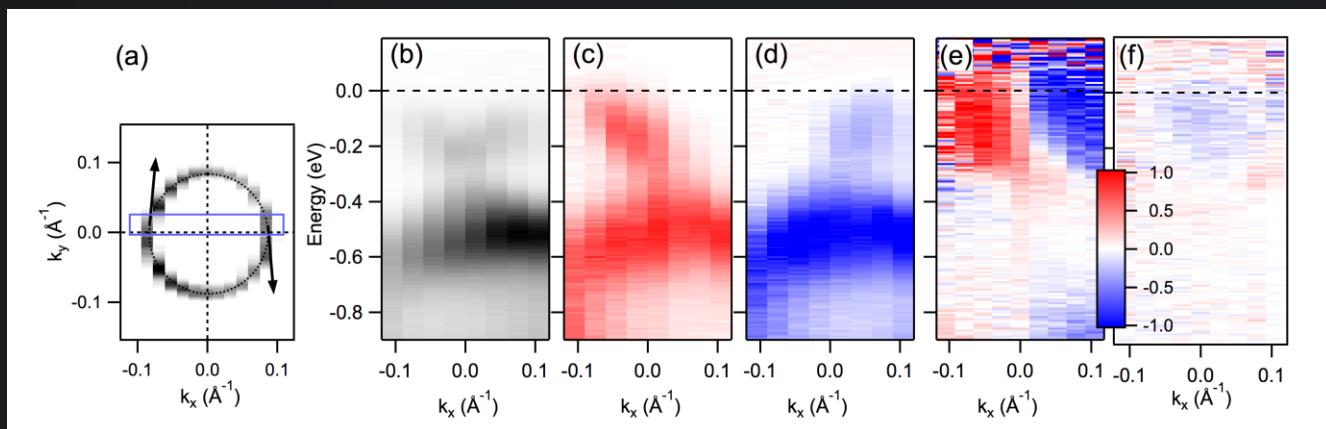
QP scattering rates

$$\Gamma_{tr}(k) = 1/\tau_{tr}(k) = 2\pi n_i \int \frac{d^2 k'}{(2\pi)^2} \delta(\varepsilon_k - \varepsilon_{k'}) |T_{kk'}|^2 (1 - \cos \theta')$$

Transport scattering rates



Spin-resolved ARPES at RT



States fully spin-polarized even at RT!

SUMMARY

Graphene:

- ~neutral graphene layers: transport - electronic structure
- Heavily doped graphene - superconductivity

Topological insulators:

- Magnetic moment of an impurity does not seem to play a role in the scattering
- Very weak e-ph coupling \Rightarrow state coherent at elevated temperatures
- State also fully polarized at room temperature
- Clean surfaces - large mobilities
- RT applications?
- New (insulating) materials!

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Samples:

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BNL

D. Gardner, S. Chu, Y. S. Lee (topological insulators)

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R. Cava (topological insulators)

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